# **University of London**

### **MSci Intercollegiate Planning Board**



## Physics MSci Student Handbook

Intercollegiate taught courses for 2006-2007 session

BPC 23<sup>rd</sup> July, 2006.

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### **Courses and Teachers**

Each course has a code number used by the Intercollegiate MSci board, shown at the left hand side. Colleges use local codes for the courses they teach. The *number* is usually the same as the MSci code, but some are different; beware! Local course codes are shown at the right hand side.

All courses are a half course unit (15 credits). In QMUL language, they are a full course unit.

The list shows the course title and the term in which it is taught. Also indicated is the course teacher and the college from where he/she comes.

No.	Course Title	Term	Teacher		Local no
4211	Statistical Mechanics	2	Prof. B. Cowan	RHUL	PH4211
4226	Advanced Quantum Theory	1	Prof. T. Monteiro	UCL	PHAS4226
4242	Relativist. Waves & Quantum Fields	2	Dr. A. Brandhuber	QMUL	PHY415
4261	Electromagnetic Theory	1	Prof. W. J. Spence	QMUL	PHY966
4317	Galaxy and Cluster Dynamics	1	Prof. M. Cropper	UCL	PHAS4317
4421	Atom and Photon Physics	1	Prof. W. R. Newell	UCL	PHAS4421
4427	Quantum Comput. and Commun.	2	Dr. S. Bose	UCL	PHAS4427
4431	Molecular Physics	2	Dr. A. Bain	UCL	PHAS4431
4442	Particle Physics	2	Dr. M. Lancaster	UCL	PHAS4442
4472	Order & Excitations in Cond. Matt.	2	Prof. D. McMorrow	UCL	PHAS4472
4473	Theor. Treatments of Nano-systems	2	Dr. A. De Vita	KCL	CP4473
4474	Physics at the Nanoscale	1	Prof. G. Davies &	KCL	CP4474
			Prof. V. Petrashov		
4478	Superfluids, Condensates and	1	Prof. J. Saunders	RHUL	PH4478
	Superconductors				
4512	Nuclear Magnetic Resonance	2	Prof. B. Cowan +	RHUL*	PH4512
4515	Computing and Statistical Data	1	Dr. G. Cowan	RHUL*	PH4515
	Analysis				
4600	Stellar Structure and Evolution	\$1	Prof. I. Williams	QMUL‡	MAS415
4601	Advanced Cosmology	1	Prof. J. Lidsey	QMUL‡	MAS401
4602	Relativity and Gravitation #	2	Dr. A. G. Polnarev	QMUL‡	MAS412
4603	Astrophysical Fluid Dynamics	2	Dr. S. Vorontsov	QMUL‡	MAS402
4630	Planetary Atmospheres	1	Dr. I. Mason	UCL	PHAS4312
4640	Solar Physics	2	Dr. I. Phillips &	UCL	PHAS4314
			Dr. van Driel		
4650	Solar System	\$2	Dr. J. Cho	QMUL‡	MAS423
4660	The Galaxy	\$2	Prof. C Murray	QMUL‡	MAS430
4670	Astrophysical Plasmas	\$1	Dr. D. Burgess	QMUL‡	ASTM116
4680	Space Plasma and Magnetospheric	2	Dr A. Coates &	UCL	PHAS4465
	Physics		Dr C. Owen		
4750	Image Capture & Sensor Technolgy	2	Dr. K. Powell	KCL	CP4750

### Students will undertake one or more project-related courses in accordance with practice at their own colleges.

- ‡ Courses taught by the *Mathematics* department of QMUL.
- \$ These QMUL courses taught in the *evening* this session.
- \* Courses taught at RHUL in Egham.
- # Course unavailable to UCL students for syllabus reasons

### Web and Email Addresses

You can communicate with most of the course teachers using email. And some courses have their own web pages. Address details are given in the following table.

No.	Course and web address	Teacher email address				
4211	Statistical Mechanics	atistical Mechanics b.cowan@rhul.ac.uk				
	http://personal.rhul.ac.uk/UHAP/027/PH42	11/				
4226	Advanced Quantum theory	t.monteiro@theory.phys.ucl.ac.uk				
4242	Relativistic Waves & Quantum Fields	a.brandhuber@qmul.ac.uk				
	http://www.strings.ph.qmul.ac.uk/~andreas	/RWQF/rwqf.html				
4261	Electromagnetic Theory	ectromagnetic Theory b.spence@qmul.ac.uk				
	http://monopole.ph.qmul.ac.uk/~bill/EMHc	mePage.html				
4317	Galaxy and Cluster Dynamics	msc@mssl.ucl.ac.uk				
4421	Atom and Photon Physics	w.r.newell@ucl.ac.uk				
4427	Quantum Computation and	s.bose@ucl.ac.uk				
	Communication	-				
4431	Molecular Physics	a.bain@ucl.ac.uk				
4442	Particle Physics	markl@hep.ucl.ac.uk				
	http://www.hep.ucl.ac.uk/~markl/teaching/	4442				
4472	Order & Excitations in Cond. Matt.	d.mcmorrow@ucl.ac.uk				
4473	Theoretical Treatments of Nano-	Alessandro.de vita@kcl.ac.uk				
	systems					
	http://www.kcl.ac.uk/kis/schools/phys_eng/phy	vsics/courses/CourseList/CP4473.htm				
4474	Physics at the Nanoscale	gordon.davies@kcl.ac.uk				
		v.petrashov@rhul.ac.uk				
	http://www.kcl.ac.uk/kis/schools/phys_eng/phy	vsics/courses/CourseList/CP4474.htm				
4478	Superfluids, Condensates and	j.saunders@rhul.ac.uk				
	Superconductors					
4512	Nuclear Magnetic Resonance	b.cowan@rhul.ac.uk				
4515	Computing & Statist. Data Analysis	g.cowan@rhul.ac.uk				
4600	Stellar Structure and Evolution	I.P.Williams@qmul.ac.uk				
4601	Advanced Cosmology	J.E.Lidsey@qmul.ac.uk				
4602	Relativity and Gravitation	A.G.Polnarev@qmul.ac.uk				
4603	Astrophysicsl Fluid Dynamics	S.V.Vorontsov@qmul.ac.uk				
4630	Planetary Atmospheres	imm@mssl.ucl.ac.uk				
4640	Solar Physics	idp@mssl.ucl.ac.uk				
	http://www.mssl.ucl.ac.uk/~lvdg/					
4650	Solar System	J.Cho@qmul.ac.uk				
4660	The Galaxy	C.D.Murray@qmul.ac.uk				
4670	Astrophysical Plasmas	D.Burgess@qmul.ac.uk				
4680	Space Plasma and Magnetospheric	ajc@mssl.ucl.ac.uk				
	Physics	cjo@mssl.ucl.ac.uk				
4750	Image Capture & Sensor Technology	keith.powell@kcl.ac.uk				
	http://www.kcl.ac.uk/kis/schools/phys_eng/phy	sics/courses/CourseList/CP4750.htm				

### **Teaching and Examination Arrangements**

**Teaching Term Dates**: Courses are taught in eleven-week terms. For the session 2006-2007 the teaching dates are:

First term Monday 2<sup>nd</sup> October 2006 – Friday 15<sup>th</sup> December 2006

Second term Monday 8<sup>th</sup> January 2007 – Friday 23<sup>rd</sup> March 2007 (Since some students won't start their second term until Monday 15<sup>th</sup> January, some courses won't start until this week. You must check the start date for each of your second term courses – details will be posted on the MSci web pages)

Note: these may not be the same as your College terms!

### **Class locations**

The timetable gives details of room locations; this is published separately from the Handbook and it is also available on the Intercollegiate MSci web pages.

Most courses are taught in lecture rooms at UCL. The exceptions are:

Courses taught at KCL 4750 Image Capture and Sensor Technology

Courses taught at QMUL

4600 Stellar Structure and Evolution
4601 Advanced Cosmology
4602 Relativity and Gravitation
4603 Astrophysical Fluid Dynamics
4650 Solar System
4660 The Galaxy
4670 Astrophysical Plasmas

*Some of these courses will be taught in the evening*; check page 3 and the timetable for details.

Courses taught at RHUL – central London base 4211 Statistical Mechanics

Courses taught at RHUL – Egham campus 4512 Nuclear Magnetic Resonance 4515 Computing & Statistical Data Analysis

### **Examination arrangements**

*UCL Students*: You will sit UCL and RHUL examinations at UCL. You will sit KCL examinations at KCL and QMUL examinations at QMUL.

*KCL Students*: You will sit KCL and RHUL examinations at KCL. You will sit UCL examinations at UCL and QMUL examinations at QMUL.

*QMUL Students*: You will sit QMUL and RHUL examinations at QMUL. You will sit UCL examinations at UCL and KCL examinations at KCL.

RHUL students: You will sit all your examinations at RHUL.

#### **Computer and Library facilities at UCL**

Students taking UCL modules may be given temporary computer accounts at UCL; your College MSci coordinator will be able to make the arrangements for you.

Most of the fourth year lectures take place in UCL lecture rooms. While you are there you might want to make use of the UCL library facilities. Your College MSci coordinator will be able to make the arrangements for you to do this.

#### University College, Gower Street, London WC1. С D А = E F G K Ξ ۵ J L Μ GOWER 1 ENDSLEIGH GARDENS n Lonsda UCLH Out-Patients GRAFTON WAY 2 STREET Private Wing STREET ENDSLEIGH Crucifor 3 4 UNIVERSITY STREET South W f Institute of Archaeology ENDSLEIGH TAVISTOCH PLACE SQUARE MORT Hut 18 5 Hut 19 SQUARE GOWE Hall 6 CAPPER STREET DMS INTLEY 43 Shropshire House Institut Connaugh GORDON GORDON 98 7 50 Morley 96 86 Church of Christ the King 97-93 Pedestrian Access ► Wheelchair Access 0 Admissions & Ge Enquiries 89 BYNG PLACE UCL Building TORRINGTON PLACE SQUARE spital Buildir 2-16 22-24 Dillon's 9 ULU

**College and Class Locations** 

Room A1, Top Floor, Physics and Astronomy building.

Through the Gower Place gateway, up steps to the second building on the left. Follow the corridor round to lift.

Room A19, Top Floor, Physics and Astronomy building.

Through the Gower Place gateway, up steps to the second building on the left. Follow the corridor round to lift.

Room D103, First Floor, 25 Gordon Street (Maths/Union building).

This is in the north-east corner of the UCL rectangle, at the corner of Gordon Street and Gower Place. It is most easily approached through the gateway in Gower Place, taking the first entrance on the left.

**Remax 2.02**: Remax House, UCL, Alfred Place, Chenies Street. This is not on the above map. Go down Gower St. past Torrington Place. Take the next right turn into Chenies Street and the first left turn into Alfred Place.

**Room 500**, Mathematics department, in Student Union building, 25 Gordon Street (beside physics).

**Queen Mary University of London**, Mile end Road, London E1. From Stepney Green station, turn left. Students may obtain a campus map from the Physics Department Secretarial office on the second floor of the Physics Building in



**Physics 112** – first floor of Physics Building (2) that is beside the Queens Building (1) as one enters the main College entrance on the Mile End Road. **Physics PLG1** – this is in the basement of the Physics Building (2). Enter the Physics Building, go straight past the lifts to the main stairwell, descend one flight and follow the corridor to the end of the building where the Lecture room entrance may be found.

**Mathematics 103** – Mathematics building (30) at West end of campus, entered from the Mile End Road. M103 is on the first floor; this room is also called the Maths Seminar Room.

**Engineering 306** – in Engineering Building (31), which is on the Mile End Road between the main entrance to the College and the Mathematics Building (30) – entrance from Mile End Road beside the People's Palace (33). Take the lift or stairs to the  $3^{rd}$  floor and then pass through the Materials Department corridor past 304 and 305 to 306 which is just at a short right –left turn in this corridor.



King's College, Strand. London, WC2.

**Room 25C**, Physics/Computer Project Laboratory: 2<sup>nd</sup> floor, Main (Old) Building. Enter the main lobby from the Strand. Take the lift to the second floor. From the lift turn right and immediately right again into the 'C' corridor of the main building (signposted). When in the main building the Physics Laboratory area is signposted as the 3<sup>rd</sup> door on the left. From this entrance area take the wooden stairs up one floor to Room 25C.

**Room Q135**, below the main quadrangle. From the main door, turn left and go down stairs to the Physics Department.

**Royal Holloway University of London**, central London base. **11 Bedford Square and 2 Gower Street**. These are two adjacent buildings on the corner of Bedford Square and Gower Street.



On arrival students must sign in at the front desk of the Bedford Square building before proceeding to their class. The Gower Street building is kept locked; the course teacher will obtain the key to the front door and students may need to ring the bell to gain entrance.

### Royal Holloway University of London, Egham campus

**By Road**: The College is on the A30, 20 miles from central London and about a mile south-west of the town of Egham. It is 2 miles from junction 13 of the M25 (London Orbital). After leaving the motorway take the A30 west, signposted to Bagshot and Camberley (not Egham). At the first roundabout, take the second exit; at the second roundabout, again take the second exit and continue on the A30 up Egham Hill. The College is on the left at the top of the hill. There are footbridges across the road at the pedestrian and main entrances.

**By Rail**: There are frequent services from London Waterloo to Egham (35 minutes); Woking to Egham (35 minutes, change at Weybridge) and Reading to Egham (40 minutes). Services at weekends, especially those on Sunday, are less frequent than on weekdays.

**By Foot**: The College is just over a mile from Egham Station, about 20 minutes walk. Turn right out of the station along Station road and walk about 100 yards to the T-Junction and the traffic lights. Turn left at the junction and follow the road up to the large roundabout; go left up Egham Hill (south-west direction). It is easiest to enter by the gate before the foot bridge over the road and follow the path to the Physics Department – buildings 21 and 22.



### 4211 Statistical Mechanics

### **The Methodology of Statistical Mechanics** (5 lectures)

- Review of equilibrium statistical mechanics.
- The grand canonical ensemble. Chemical potential. The Bose and Fermi distribution functions.
- The classical limit, phase space, classical partition functions.

### Weakly Interacting Systems (7 lectures)

- Non-ideal systems. The imperfect gas and the virial expansion, Mayer's *f* function and cluster integrals. (2 lectures)
- The second virial coefficient for the hard sphere, square-well and Lennard-Jones potentials. (2 lectures)
- Throttling and the Joule-Kelvin coefficient. (1 lecture)
- Details of the van der Waals gas and the mean field theory for magnetic systems. (2 lectures)

### Strongly Interacting Systems (13 lectures)

- The phenomenology of phase transitions, definitions of critical exponents and critical amplitudes. (2 lectures)
- Scaling theory, corresponding states. (2 lectures)
- Introduction to the Ising model. Magnetic case, lattice gas and phase separation in alloys and Bragg-Williams approximation. Transfer matrix method in 1D. (3 lectures)
- Landau theory. Symmetry breaking. Distinction between second order and first order transitions. Discussion of ferroelectrics. (3 lectures)
- Broken symmetry, Goldstone bosons, fluctuations, scattering, Ornstein Zernike, soft modes. (3 lectures)

### **Dissipative Systems** (5 lectures)

• Fluctuation-dissipation theorem, Brownian motion, Langevin equation, correlation functions. (5 lectures)

### Books:

B. Cowan, "Topics in Statistical Mechanics", 2005, Imperial College Press.
R. Bowley & M. Sánchez, "Introductory Statistical Mechanics", 1999, OUP
Other books and publications will be referred to by the lecturer.
Course notes and other material available on the course web pages at http://personal.rhul.ac.uk/UHAP/027/PH4211/

### Assessment:

Written examination of 2<sup>1</sup>/<sub>2</sub> hours contributing 90%, coursework contributing 10%.

### 4226 Advanced Quantum Theory

The module consists of 30 lectures. These will be used to cover the syllabus material and to discuss problem sheets as the need arises. The approximate allocation of lectures to topics is shown in brackets below.

## Basic ideas of quantum mechanics (partly revision) and formal quantum mechanics[5]

(Formal aspects of quantum theory are distributed throughout the course and introduced as needed.)

Bras and kets, states, operators, Born interpretation of the wave function, continuous and discrete eigenvalues, Dirac delta function, compatible observables, Hermitian and unitary operators, Dirac notation, closure relation, time-evolution, Schrödinger, Heisenberg and interaction pictures, transformation brackets, momentum representation.

### Angular momentum (partly revision) [5]

Angular momentum operators, commutation algebra, raising and lowering operators, spectrum of angular momentum eigenvalues, combination of angular momenta treating the simplest case of two spin-1/2 particles, notation of Clebsch-Gordan coefficients, spin-1/2 angular momentum and Pauli matrices.

### *Non-perturbative approximations* [4]

The JWKB approximation. Examples.

### *Time-dependent perturbation theory* [7]

First-order time-dependent perturbation theory. Harmonic perturbations and other applications of time-dependent perturbation theory. Second-order perturbation theory and energy denominators. First Born approximation from the dependent approach. Fermi's Golden Rule.

### Scattering [9]

Currents and cross sections; the scattering amplitude and the optical theorem. Partial wave expansion of wave function and scattering amplitude. Phase shifts. Low-energy scattering from square well potential and scattering length expansion. Scattering length expansion in terms of wave functions. Poles of the scattering amplitude, bound states and resonances. First Born approximation from the time-independent approach. Integral equation for potential scattering.

### **Books:**

Those which are closest to the material and level of the course are (in alphabetical order)

- *Introduction to Quantum Mechanics*, B.H. Bransden and C.J.Joachain, Longman (2<sup>nd</sup> Ed, 2000), ) (available at a discount from the physics departmental Tutor),
- Quantum Mechanics, (2 Vols) C.Cohen-Tannoudji, B.Diu and F.Laloe, Wiley,
- Quantum Physics, S.Gasiorowicz, Wiley (1996),
- Quantum Mechanics, F.Mandl, Wiley (1992),
- Quantum Mechanics, E.Merzbacher, (3rd Ed.) Wiley, (1998

Assessment: Examination of 2<sup>1</sup>/<sub>2</sub> hours duration contributing 100%.

### **Prerequisites:**

The following topics will be assumed to have been covered:

**Introductory material**: states, operators and the Born interpretation of the wave function, transmission and reflection coefficients;

**Harmonic oscillator**: by the differential equation approach giving the energy eigenvalues and wave functions;

**Angular momentum**: angular momentum operators and the spectrum of eigenvalues, raising and lowering operators; the spherical harmonics and hydrogenic wave functions;

**Time-independent perturbation theory**: including the non-degenerate and degenerate cases and its application to the helium atom ground state, Zeeman effect and spin-orbit interactions.

### Aims of the Course

This course aims to:

- review the basics of quantum mechanics so as to establish a common body of knowledge for the students from the different Colleges on the Intercollegiate M.Sci. programme;
- extend this by discussing these basics in more formal mathematical terms;
- develop the JWKB method for non-perturbative approximations;
- discuss the addition of angular momentum and Clebsch-Gordan coefficients;
- introduce time-dependent perturbation theory ;
- discuss the quantum mechanical description of the non-relativistic potential scattering of spinless particles in terms of the partial wave expansion and the Born approximation;
- provide the students with basic techniques in these areas which they can then apply in specialist physics courses.

### 4242 Relativistic Waves and Quantum Fields

**Quantum Mechanics and Special Relativity (part revison)**: (6 hours) Schroedinger equation, wavefunctions, operators/observables, pictures, symmetries and conservation laws in QM; short introduction to Special Relativity: 4-vector notation, Lorentz transformations, Lorentz invariance/covariance, Lorentz transformation of the electromagnetic field

### **Relativistic Wave equations**: (10 hours)

Klein-Gordon equation and probability density; Dirac equation, covariance and probability density, non-relativistic limit, spin, Feynman notation, plane wave solutions, Lorentz transformations of plane wave solutions; hole theory and antiparticles, vacuum polarisation; discrete symmetries: C & P & T symmetry and their relevance for electromagnetic and weak interactions, Dirac covariants; wave equations for massless fermions, neutrinos; Feynman interpretation of the Klein-Gordon equation; Dirac equation in an electromagnetic field, magnetic moment of electron, relativistic spectrum of Hydrogen atom.

### Quantum Field Theory: (17 hours)

Classical field theory, Noether theorem, stress-energy tensor, symmetries and conserved currents; canonical quantisation of the Klein-Gordon field, creation and annihilation operators, vacuum energy, Casimir energy; quantisation of Dirac fermion, spin- statistics connection; commutators and time ordered products, the Feynman propagator; Dyson expansion; S-matrix, scattering amplitudes, transition rates; cross sections;  $\Phi^4$ -theory scattering amplitude; decay rates of unstable particles; Wick's theorem and its application to perturbation theory, Feynman rules; quantisation of electromagnetic field and Gupta-Bleuler formalism; interaction with electron; Feynman rules & various scattering processes: Compton, electron-electron, electron-positron; cross sections and spin sums.

Four sessions will be devoted to a discussion of coursework problems and their solutions.

### **Prerequisites**: 3<sup>rd</sup> year Quantum course

### Books:

F. Mandl and G. Shaw, "Quantum Field Theory", John Wiley and Sons Ltd L.H. Ryder, "Quantum Field Theory", Cambridge University PressJ. Bjorken and S. Drell, "Relativistic quantum mechanics" and "Relativistic quantum fields", McGraw-HillS. Weinberg, "The Quantum Theory of Fields", Volume I, Cambridge University Press

### Assessment:

Written examination of 2<sup>1</sup>/<sub>2</sub> hours contributing 90%, coursework contributing 10%.

### 4261 Electromagnetic Theory

- Revision of laws of electromagnetism *in vacuo*, displacement current, Maxwell's equations *in vacuo*, charge and current density sources, energy theorems, fluxes of energy and momentum. (2 hours)
- Polarization and magnetization, **D** and **H** fields, linear media, boundary conditions on the fields in media, Maxwell stress tensor, concept of macroscopic fields as space averages of molecular fields, Lorentz local field argument, the Clausius-Mossotti relation. (3 hours)
- Maxwell's equations in media, Homogeneous wave equation *in vacuo* and in media, concept of frequency dependent dielectric function  $\varepsilon(\omega)$ , properties of real and imaginary parts of  $\varepsilon(\omega)$ , causality, Kramers-Krönig relation. (3 hours)
- Scalar and vector potentials, gauge transformations, inhomogeneous wave equation, the retarded solution to the wave equation, radiation from a Hertzian dipole with discussion of near and far fields, formula for power radiated, qualitative discussion of magnetic dipole and electric quadrupole radiation. (4 hours)
- Scattering of a plane wave by a single slowly moving charged particle, total and differential scattering cross-sections, optical theorem, scattering from a medium with space-varying dielectric constant, scattering from an assemblage of polarizable particles, Rayleigh-Smoluchowski-Einstein theory of why the sky is blue critical opalescence. (5 hours)
- Lorentz transformations, charge and current density as a 4-vector, the potential 4-vector, tensors and invariants, the relativistic field tensor  $F^{\mu\nu}$ , Lorentz transformation properties of current density and potential 4-vectors and of the free vacuum **E** and **B** fields, tensor form of Maxwell's equations, covariant formulation of energy and momentum theorems, energy-momentum tensor. (5 hours)
- Liénard-Wiechert potentials for a moving charged particle derived from a deltafunction source, fields for a uniformly moving charged particle in the nonrelativistic and ultra-relativistic limits, radiation from accelerated charges, the cases of velocity and acceleration parallel and perpendicular, Larmor formula for radiated power, bremsstrahlung and synchrotron radiation as examples. (5 hours)
- Maxwell theory as a Lagrangian field theory, the free field as an ensemble of oscillators. (3 hours)

### **Prerequisites:**

The course assumes a knowledge of the electromagnetism topics as detailed in the Institute of Physics Recommended Core. These comprise:

- Electrostatics: the electric field **E**
- Charge. Coulomb's law, Gauss's flux theorem
- Electrostatic potential; Poisson's and Laplace's equations
- The field and potential of a point charge and an electric dipole
- Capacitance and stored energy
- Magnetostatics: the magnetic field **B**
- Electric currents; the Biot-Savart law, Ampère's circuital theorem
- The field of a linear current and of a magnetic dipole/current loop
- Lorentz force law, force on current-carrying conductors
- Motion of particles in electric and magnetic fields
- Electrodynamics: Faraday's law, Lenz's law and induction
- Inductance and stored magnetic energy
- Maxwell's equations and electromagnetic waves
- The electromagnetic spectrum
- The Poynting vector
- Fields in media: **D** and **H**; permittivity, permeability and dielectric constant: basic ideas, related to their microscopic origins
- Energy storage in media

In addition the following knowledge in mathematics and physics are assumed:

- Taylor series.
- Div, Grad and Curl, Surface and Volume integrals, Gauss and Stokes theorems.
- The complex representation of harmonically varying quantities.
- Fourier transforms.
- The one-dimensional wave equation.
- Matrix multiplication and familiarity with indices.
- Contour integration up to Cauchy's theorem (this is used only in the discussion of the Kramers-Krönig relation)
- From special relativity the explicit form of the simple Lorentz transformation between frames in relative motion along a single coordinate direction.
- It is desirable but not necessary that students have met the Lagrangian formulation of particle mechanics.
- We do not assume that students have met the concept of Green's functions before.

### **Books:**

J D Jackson, "Classical Electrodynamics", J Wiley H C Ohanian, "Classical Electrodynamics", Allyn and Bacon

### Assessment:

Written examination of 2<sup>1</sup>/<sub>2</sub> hours contributing 90%, coursework contributing 10%.

### 4317 Galaxy and Cluster Dynamics

### Galaxies, Clusters and the Foundations of Stellar Dynamics [5]

Observational overview of extragalactic astronomy The classification of galaxies, star clusters, clusters of galaxies Characteristics of the Milky Way and other galaxies The uses of stellar dynamics. The equations of motion and the Collisionless Boltzmann Equation. Isolating integrals and Jeans' theorem

### The Structure of the Milky Way [8]

Galactic co-ordinates, the local standard of rest and rotation curves. Differential rotation, Oort's constants, epicyclic motions. Motions perpendicular to the galactic plane. The third integral - 'box' and 'tube' orbits. Local galactic dynamics; star-streaming, Jeans' equations. Asymmetric drift. The gravitational field of the Milky Way. The growth of instabilities, spiral structure, the density wave theory

### Stellar Encounters and Galactic Evolution [4]

The effects of distant stellar encounters, two-body relaxation. The Fokker-Planck approximation, dynamical friction. The virial theorem and its applications

### Star Clusters [5]

The dynamics of clusters; evaporation, the King model. The effects of tidal forces. Dynamical evolution and core collapse

### **Elliptical Galaxies** [4]

Collisionless relaxation: phase damping and violent relaxation. Shapes and intensity profiles. Dynamical models; orbit families. Mergers and the origin of elliptical galaxies

### Clusters of Galaxies [4]

The description of clustering, the Local Group. Dynamics of clusters of galaxies, formation timescales. The determination of galactic masses. The missing mass problem.

**Books**: Stellar Dynamics (I.R. King, W.H. Freeman, 1996) Galaxies: Structure and Evolution (R.J. Tayler, Cambridge Univ. Press, 1993)

Assessment: Written examination of 2<sup>1</sup>/<sub>2</sub> hours contributing 100%

**Prerequisite**: UCL's ASTR3C36 - Cosmology and Extragalactic Astronomy or equivalent.

### 4421 Atom and Photon Physics

### **Interaction of Light with atoms (single photon)** (4 lectures)

- 1 Processes excitation, ionization, auto-ionization
- 2 A and B coefficients (semi classical treatment)
- 3 Oscillator strengths and *f*-sum rule
- 4 Life times experimental methods. (TOF and pulsed electron)
- 5 Review of selection rules
- 6. Photo-ionization synchrotron radiation

### L.A.S.E.R (3 lectures)

- 1 Line shapes g(v); Pressure, Doppler, Natural
- 2 Absorption and Amplification of radiation
- 3 Population inversion; spontaneous and stimultated emission
- 4 YAG and Argon ion lasers
- 5 Tunable radiation dye and solid
- 6 Mode structure

### **Chaotic Light and Coherence** (2 lectures)

- 1 Line broadening
- 2. Intensity fluctuations of chaotic light
- 3 First order correlation functions
- 4. Hanbury Brown Twiss experiment

### Laser Spectroscopy (3 lectures)

- 1 Optical pumping orientation and alignment
- 2 Saturation absorption spectroscopy
- 3 Lamb shift of H(1S) and H(2S)
- 4 Doppler-Free spectroscopy

### Multi-Photon Processes (3 lectures)

- 1 Excitation, ionization, ATI
- 2 Laser field effects pondermotive potential Stark shifts Harmonic Generation
- 3 Pump and Probe Spectroscopy
- 4 Multi-photon interactions via virtual and real states
- 5 Two photon decay of hydrogen (2S–1S)
- 6 Simultaneous electron photon interactions

### Light Scattering by Atoms (3 lectures)

- 1 Classical Theory
- 2 Thompson and Compton scattering
- 3 Kramers-Heisenberg Forumlae
- 4 (Rayleigh and Raman scattering)

### **Electron Scattering by Atoms** (4 Lectures)

- 1 Elastic, inelastic and super-elastic
- 2 Potential scattering
- 3 Scattering amplitude partial waves

- 4 Ramsauer-Townsend Effect Cross Sections
- 5 Resonance Structure

### **Coherence and Cavity Effects in Atoms** (4 lectures)

- 1 Quantum beats beam foil spectroscopy
- 2 Wave packet evolution in Rydberg states
- 3 Atomic decay in cavity
- 4. Single atom Maser

### **Trapping and Cooling** (4 lectures)

- 1 Laser cooling of atoms
- 2 Trapping of atoms
- 3 Bose condensation
- 4 Physics of cold atoms Atomic Interferometry

### Books:

A Thorne, "Spectrophysics", (Chapman and Hall) J Wilson and J F B Hawkes, "Opto Electronics", (Prentice Hall)

### Assessment:

Written examination of  $2\frac{1}{2}$  hours contributing 100%.

### 4427 Quantum Computation and Communication

**Background** [3]: The qubit and its physical realization; Single qubit operations and measurements; The Deutsch algorithm; Quantum no-cloning.

**Quantum Cryptography** [3]: The BB84 quantum key distribution protocol; elementary discussion of security; physical implementations of kilometers.

**Quantum Entanglement** [8]: State space of two qubits; Entangled states; Bell's inequality; Entanglement based cryptography; Quantum Dense Coding; Quantum Teleportation; Entanglement Swapping; Polarization entangled photons & implementations; von-Neumann entropy; Quantification of pure state entanglement.

**Quantum Computation** [8]: Tensor product structure of the state space of many qubits; Discussion of the power of quantum computers; The Deutsch-Jozsa algorithm; Quantum simulations; Quantum logic gates and circuits; Universal quantum gates; Quantum Fourier Transform; Phase Estimation; Shor's algorithm; Grover's algorithm.

**Decoherence & Quantum Error Correction** [4]: Decoherence; Errors in quantum computation & communication; Quantum error correcting codes; Elementary discussion of entanglement concentration & distillation.

**Physical Realization of Quantum Computers** [4]: Ion trap quantum computers; Solid state implementations (Kane proposal as an example); NMR quantum computer.

Books:

Assessment: Written examination of 2<sup>1</sup>/<sub>2</sub> hours contributing 100%

Prerequisites: Third year level quantum mechanics.

### 4431 Molecular Physics

### **1.** Atomic Physics (2 lectures)

Brief recap of atomic physics: n, l, m, s; He atom, orbital approximation, exchange.

### 2. Molecular electronic structure (8 lectures):

The molecular Hamiltonian and the Born-Oppenheimer approximation.

Electronic structure, ionic and covalent bonding, Bonding in  $H_2^+$  and  $H_2$ . Muon catalysed fusion. Dissociation and united atom limits. Long range forces.

### **3.** Nuclear motion (6 lectures)

Vibrational structure: harmonic motion and beyond, energy levels and wavefunctions Rotational structure: rigid rotor and energy levels Energy scales within a molecule: ionisation and dissociation. Nuclear spin effects. Labeling schemes for electronic, vibrational and rotational states.

### **4.** Molecular spectra (7 lectures):

Microwave, infrared and optical spectra of molecules. Selection rules, Franck-Condon principle. Experimental set-ups. Examples: the  $CO_2$  laser, stimulated emission pumping experiment. Raman spectroscopy. Ortho-para states. Absorption spectra of simple diatomics (eg  $O_2$  and NO,  $N_2$ ). Simple poly-atomics (ozone, water).

### **5.** Molecular processes (7 lectures):

Collisions with electrons. Elastic and inelastic collisions. Dissociation, dissociative attachment and dissociative recombination. Resonances and negative ions. Experimental techniques. Theoretical models (briefly).

**Prerequisites**: Quantum Physics (year 2/3), Atomic Physics (year 2/3), some previous experience of basic molecular physics would be helpful but is not a requirement.

### Books:

P W Atkins and R S Friedman, "Molecular Quantum Mechanics", (Oxford University)

B H Bransden and C J Joachain, "Physics of Atoms and Molecules", (Longman, 1983)

C.W. Banwell and E. McGrath, "Fundamentals of Molecular Spectroscopy", 4<sup>th</sup> Edition, (McGraw-Hill, 1994)

### Assessment:

Written examination of  $2\frac{1}{2}$  hours contributing 100%

### 4442 Particle Physics

### **Basic Concepts**

Four vector notation, invariants and natural units. Feynman diagrams as a tool for qualitative description of interactions. Cross sections, differential cross sections and luminosity. The Mandelstam variables s, t and u for scattering. The family of fundamental particles: leptons and quarks and vector bosons. Interactions of leptons and quarks, summarised in terms of characteristic decay times, ranges and the mediating bosons. Yukawa field.

### **Relativistic QM**

Relativistic wave equations (Klein-Gordon, Dirac). Negative energy solutions and the Feynmann-Stuckelberg interpretation. Conserved Current and Propagators. Invariant amplitude.

### Symmetries and conservation laws.

Translational invariance and momentum conservation as a worked example. Symmetries of the Strong and Electromagnetic Interactions: Relation between symmetry, invariance and conservation laws; parity (invariance of Hamiltonian, fermions and antifermions, quarks and hadrons). Higgs mechanism and spontaneous symmetry breaking.

### **Particle Detectors**

These will be covered as an integral part of the study of current experiements. Basic principles of calorimeters, drift chambers and silicon vertex detectors.

### **Leptons and Hadrons**

Discovery of leptons. Evidence for lepton universality, lepton number conservation. Parity, C Symmetry. Quarks, and hadrons. Multiplets and Quark diagrams. Resonances. Breit-Wigner formula.

### Quarks and QCD

Colour. Confinement. Screening, Asymptotic freedom and Jets. Rhad for  $e^+e^-$  annihilation. 2- and 3-jet events. The discovery of the top quark through the measurement of jets at the CDF detector at Fermilab, including a look at basic calorimetry.

### More on Leptons, and Weak Interactions

Discovery and properties of W and Z bosons. Quark and lepton doublets and Cabibbo mixing. Comparing the weak and electromagnetic couplings. Parity and C-Parity violation and handedness of neutrinos. The measurement of Z width at LEP. Electroweak Theory: Unification of weak and electromagnetic. Gauge transformations.

### **Deep Inelastic Scattering**

Elastic electron-proton scattering. Deep Inelastic scattering. Scaling and the quark parton model. Factorisation. Scaling violations and QCD. Triggering at HERA. Measurement of proton structure at HERA. Neutral and Charged Currents at HERA.

### The Standard Model and What Next?

Some idea of current open questions. Neutrino oscillations, running couplings, SUSY. Cosmological connections – dark matter, CP violation, very high energy cosmic rays.

Prerequisites: 4241 Relativistic Quantum Mechanics, Atomic and Nuclear (year 2/3)

### Books:

B R Martin and G Shaw, "Particle Physics", J. Wiley Halzen and Martin, "Quarks and Leptons", J. Wiley D H Perkins, "Introduction to High Energy Physics", Addison-Wesley.

### Assessment:

Written examination of  $2\frac{1}{2}$  hours contributing 100%

### 4472 Order and Excitations in Condensed Matter

### **Syllabus**

The allocation of topics to sessions is shown below. Each session is approximately three lectures.

*Atomic Scale Structure of Material* (session 1): The rich spectrum of condensed matter; Energy and time scales in condensed matter systems; Crystalline materials: crystal structure as the convolution of lattice and basis; Formal introduction to reciprocal space.

*Magnetism: Moments, Environments and Interactions* (session 2) Magnetic moments and angular momentum; diamagnetism and paramagnetism; Hund's rule; Crystal fields; Exchange interactions

*Order and Magnetic Structure* (session 3) Weiss model of ferromagnetism and antiferromagnetism; Ferrimagnetism; Helical order; Spin Glasses; Magnetism in Metals; Spin-density waves; Kondo effect

*Scattering Theory* (sessions 4 and 5) X-ray scattering from a free electron (Thomson scattering); Atomic form factors; Scattering from a crystal lattice, Laue Condition and unit cell struture factors; Ewald construction; Dispersion corrections; QM derivation of cross-section; Neutron scattering lengths; Coherent and incoherent scattering

*Excitations of Crystalline Materials* (session 6) Dispersion curves of 1D monoatomic chain (revision); Understanding of dispersion curves in 3D materials; Examples of force constants in FCC and BCC lattices; Dispersion of 1D diatomic chain; Acoustic and Optic modes in real 3D systems; Phonons and second quantization; Anharmonic interactions

*Magnetic Excitations* (session 7) Excitations in ferromagnets and antiferromagnets; Magnons; Bloch  $T^{3/2}$  law; Excitations in 1, 2 and 3 dimension; Quantum phase transitions

*Sources of X-rays and Neutrons* (session 8) Full day visit to RAL. Neutron Sources and Instrumentation. Synchrotron Radiation. Applications of Synchrotron Radiation

### Modern Spectroscopic Techniques (session 9)

Neutron scattering: triple-axis spectrometer, time-of-flight, polarized neutrons X-ray scattering: X-ray magnetic circular dichroism, resonant magnetic scattering, reflectivity

*Phase transitions and Critical Phenomena* (session 10) Broken symmetry and order parameters in condensed matter. Landau theory and its application to structural phase transitions, ferromagnetism, etc. Ising and Heisenberg models. Critical exponents. Universality and scaling

*Local Order in Liquids and Amorphous Solids* (session 11) Structure of simple liquids; Radial distribution function; Dynamics: viscosity, diffusion; Modelling; Glass formation; Simple and complex glasses; Quasi-crystals

### Textbooks

Main texts: Structure and Dynamics: An Atomic View of Materials, Martin T. Dove (OUP); Magnetism in Condensed Matter, Stephen Blundell (OUP) Additional texts: Elements of Modern X-ray Physics, Jens Als-Nielsen and Des McMorrow (Wiley); Introduction to the Theory of Thermal Neutron Scattering, G.L. Squires (Dover)

### Assessment

Written examination of 2<sup>1</sup>/<sub>2</sub> hours contributing 100%

### Prerequisites

UCL's PHYS3C25 – Solid State Physics, or an equivalent from another department

### 4473 Theoretical Treatments of Nano-systems

### Overall aim of the course:

An increasing amount of science and technology is nowadays concerned with processes at the nanometer scale, typically involving functionalized structures like particles and molecules. Time scales of picoseconds are the natural ones to describe the vibrational/conformational properties of these systems, and the relevant steps of their synthesis/assembly mechanisms. Such a high time/size resolution poses extremely demanding constraints to experimental techniques.

A detailed theoretical description and quantum-based numerical modelling have thus become indispensable tools in modern research on this systems, as guides for interpreting the experimental observations and, increasingly, as independent complementary investigation tools, capable of quantitative predictions. The relevant physics at the nanoscale is quantum mechanics, and quantum approaches must be used to provide the potential energy surfaces and the structural/configurational properties which are at the basis of classical molecular dynamics techniques and phase-space descriptions.

This course provides an introduction to the rapidly growing area of atomistic-based theoretical modelling in nano-science, based on fundamental quantum theory. The course introduces the physics of many-electron systems with a particular focus on symmetry properties and on the simplifying assumptions which must be used to successfully model functional nanosized systems. While a main goal of the course is to provide a theoretical background on the structure and quantum behaviour of matter at the nano-scale, examples of applications given during the course involve modern concepts on the nano-scale behaviour of functional materials, and provide an accessible introduction to some of the main theoretical techniques used to model processes involving surfaces, interfaces, clusters, and macromolecules.

### **Objectives**:

On successfully completing this course, a student should:

- Be familiar with the fact that the physical properties of complex nano-systems can be described within a coherent quantum mechanical framework, in particular that the many-electron QM problem can be attacked by mean-field techniques of different levels of complexity
- Understand how this theoretical description can be used as a basis for modelling tools yielding accurate quantum-based potential energy surfaces and inter-atomic force models, and thus is capable of quantitative predictions at the nanometer/picosecond size- and time- scales.

### **Topics**:

### (1) Foundations: mean-field modelling of many electron systems.

The many-body problem: the general Schroedinger equation problem. The particle exchange operator, symmetry of a two-body wave function with spin. Wavefunction classes constructed from spin orbitals. Reminder of perturbation theory.

Reminder of variational techniques. Example: the virial theorem for Coulombic systems. Variational minimum obtained through self-consistency: derivation of a

simple self-consistent Hartree equation for the Helium ground state. Correlation energy. Many electrons: symmetry of the many body wave function under particle exchange. Pauli principle and Slater determinants. The general Hartree-Fock method (outline), electronic correlation in many electron systems. Modern self-consistent approaches: elements of Density Functional Theory.

### (2) Potential energy surfaces and molecular dynamics.

Quantum molecules: the hamiltonian operator, the Born-Oppenheimer approximation, degrees of freedom of the electronic energy, reminder of the molecular roto-vibration spectrum. The Hellman-Feynman theorem and the concept of classical interatomic force-field. The Verlet Algorithm and First-Principles Molecular Dynamics. Classical potentials, the problem of transferability.

Modelling free energy barriers via thermodynamic integration. Classical dynamics and stochastic processes. Modelling the diffusion of point defects in crystalline solids. The central limit theorem and the evolution of a distribution function. The diffusion coefficient. Derivation of Fick's laws. Examples and exercises.

### (3) Electronic structure, symmetry, case studies.

Approximate representations for the electronic structure of large molecular systems, derivation of a simple tight-binding scheme (LCAO in the nearest neighbour approximation). The case of aromatic n-rings: model energy multiplets in aromatic systems: HOMO and LUMO levels and the prediction of STM images in negative/positive bias.

The connection between finite and infinite systems: the infinite 1D periodic solid and direct calculation of a model band structure. Bloch states, the Bloch theorem in Born-Von Karman periodic conditions. Other notable symmetries.

If time allows, case study (updated each year), e.g. self-assembly of 2D nanostructures. Construction of a classical force-field and molecular dynamics.

### **Reading List**

1. B. H. Bransden and C. J. Joachain, "Physics of Atoms and Molecules", Prentice Hall (2002) ISBN: 058235692X

2. M. Finnis, "Interatomic Forces in Condensed Matter", Oxford University Press (2003) ISBN: 0198509774

3. M. P. Allen and D. J. Tildesley, "Computer Simulations of Liquids", Clarendon Press (1989) ISBN: 0198556454

4. D. Frenkel and B. Smit, "Understanding Molecular Simulations", Academic Press (2001) ISBN: 0122673514

### Assessment:

Written examination contributing 90% of the total marks. Coursework contributing 10%

### **Pre-requisites**:

CP3221 Spectroscopy and Quantum Mechanics, or equivalent

### 4474 Physics at the Nanoscale

### Overall aim of the course:

Today an increasing amount of science and technology is concerned with processes at the nano-scale, typified by structures of the order of 10 nanometre in dimension. At this scale, physics is determined by quantum processes, and not by the random (or statistical) processes that dominate in systems of larger sizes. This course provides an introduction to the rapidly growing area of nano-science. Already, nano-structures are 'familiar' to us in the structure of the current generation of computer chips, and the applications of nano-structures are predicted to contribute to the new technologies of this century.

The course introduces the physics and chemistry of nano-structures, discusses their special properties, methods of fabricating them, and some of the methods of analysing them.

### **Objectives:**

On successfully completing this course, a student should:

Appreciate the difference between the physics on the classical (macro-) scale and on the quantum (nano-) scale.

Understand the properties of nanostructures in 'zero', one and two dimensions, their fabrication and their characterisation.

### **Topics:**

### Definitions of the nano-scale: the importance of precise structures. Reminder of some key properties of metals / semiconductors:

Band states, dependence of electron energy on k2, density of electron states. Fermi surface. Example of use of ideas in de Haas van Alphen effect. Effective mass. Concept of a hole. Excitons in semiconductors.

### Introduction to a classic semiconductor nano-science

Example – GaAs/AlGaAs structures.

Their fabrication by molecular beam epitaxy.

### Electrons in a two-dimensional layer:

Quantum mechanics (particle in a box).

Density of electron states.

Verification of energy levels by optical measurements.

Quantum Hall effect.

Superlattices.

### Electrons in a one-dimensional system: formation in GaAs/AlGaAs.

Density of states.

Diffusive and ballistic conduction.

Quantised conduction.

### Quantum dots:

Fabrication and control of growth in semiconductor/insulator systems by epitaxial processes and by ion-implantation.

Overview of making low-dimensional structures in semiconductor materials: what can be achieved in terms of purity and size control.

The importance of strain as a limit of strained-layer growth, and the use of strain in strain-engineering.

### Characteristic sizes:

Characteristic length scales.

Single electron effects on the capacitance and current; Coulomb blockade.

Quantum interference of conduction electrons.

Aharonov-Bohm effect.

Universal conductance fluctuations.

### 'Top down' fabrication:

Thin layer deposition techniques by thermal evaporation, laser ablation, chemical vapour deposition and MOCVD, plasma-assisted deposition (ECR and Helicon regimes), ion-implanted layers.

### 'Bottom up' fabrication:

Scanning probe based nano-technology, molecular manufacturing. Self-organised nano-structures.

### Nano-lithography:

Resolution limits.

Electron-beam lithography.

Proximity effect.

Negative and positive lithographic processes.

Electron beam resists.

Ion beam etching and RIBE.

Plasma-assisted etching.

Alignment and self-alignment.

X-ray lithography.

Ion-beam lithography.

### Nano-analysis:

SEM- and STEM-based methods.

X-ray and electron spectroscopy.

Scanning tunneling microscopy.

Atomic force microscopy and other scanning probe-based methods, including scanning near field optical microscopy.

### Confocal microscopy.

### Clean-room environment. The present. (updated each year).

### Assessment:

one three hour examination, worth 90% of the total marks. Two sets of marked coursework, both of which count equally at 5% each of the total marks.

### **Pre-requisites:**

Quantum mechanics at a typical second year level is essential. Condensed matter physics at a typical third year level is desirable but not essential.

### 4478 Superfluids, Condensates and Superconductors

The extraordinary properties of Superfluids, Superconductors and Bose-Einstein condensates are fascinating manifestations of macroscopic quantum coherence: the fact that the low temperature ordered state is described by a macroscopic wavefunction.

We will study quantum fluids, the superfluidity of liquid <sup>4</sup>He and liquid <sup>3</sup>He, Bose-Einstein Condensation in dilute gases, metallic superconductivity, as well as the different techniques for achieving low temperatures. It is hoped to emphasize the conceptual links between these very different physical systems. Important developments in this subject were recognised by Nobel prizes in 2003, 2001, 1997, 1996, 1987, 1978, 1973, 1972, 1962 and 1913, which is one measure of its central importance in physics.

### Introduction and review of quantum statistics.

The statistical physics of ideal Bose and Fermi gases.

### Superfluid <sup>4</sup>He and Bose-Einstein condensation.

Phase diagram. Properties of superfluid <sup>4</sup>He. Bose-Einstein condensation in <sup>4</sup>He. The two-fluid model and superfluid hydrodynamics. Elementary excitations of superfluid <sup>4</sup>He. Breakdown of superfluidity. Superfluid order parameter: the macroscopic wavefunction. Quantization of circulation and quantized vortices. Rotating helium.

### Bose-Einstein condensation in ultra-cold atomic gases

Cooling and trapping of dilute atomic gases. BEC. Interactions. Macroscopic quantum coherence. Rotating condensates and vortex lattices. The atom laser.

### Liquid <sup>3</sup>He; the normal Fermi liquid.

Phase diagram. Properties of normal <sup>3</sup>He. Quasiparticles. Landau theory of interacting fermions.

### Liquid solutions of <sup>3</sup>He and <sup>4</sup>He.

Isotopic phase separation. Spin polarised <sup>3</sup>He.

### The properties of quantum fluids in two dimensions

Two dimensional Fermi systems. The superfluidity of 2D <sup>4</sup>He; the Kosterlitz-Thouless transition.

### Achieving low temperatures

<sup>3</sup>He-<sup>4</sup>He dilution refrigerator. Adiabatic demagnetisation of paramagnetic salts. Nuclear adiabatic demagnetisation. Pomeranchuk cooling.

### Measurement of low temperatures

Thermal contact and thermometry at tremperatures below 1K.

### Superfluid <sup>3</sup>He.

Superfluid <sup>3</sup>He as a model p-wave superfluid. Discovery and identification of the superfluid ground states. <sup>3</sup>He-A, the anisotropic superfluid.

### Superconductivity

Review of the basic properties of superconductors. Meissner effect. Type I and type II superconductors. Pairing in conventional and unconventional superconductors. Survey of recent advances in novel superconductors.

### The Josephson effects.

Josephson effects in superconductors, superfluid <sup>4</sup>He and superfluid <sup>3</sup>He.

### **Prerequisites**:

This course requires knowledge of base level thermodynamics and statistical physics at year 2/3 level and quantum mechanics at typical year 2 level. A background in solid state physics and superconductivity as covered in a typical year 3 condensed matter course is desirable but not essential.

### Books:

Course notes, popular articles, scientific articles and review articles, web based material.

J F Annett, Superconductivity, Superfluids and Condensates, Oxford University Press (2004)

Tony Guénault, Basic Superfluids, Taylor and Francis (2003)

D R Tilley and J Tilley, "Superfluidity and Superconductivity" Adam Hilger. P M<sup>c</sup>Clintock, D J Meredith and J K Wigmore, "Matter at Low Temperatures" 1984, Blackie. (Out of print).

J Wilks and D S Betts, "An Introduction to Liquid Helium" 1987, Oxford (out of print).

### Assessment:

Written examination of  $2\frac{1}{2}$  hours contributing 80%, coursework and essays contributing 20%.

### 4512 Nuclear Magnetic Resonance

In Session 2006-7 this course will be taught at the Royal Holloway campus at Egham

This course will introduce students to the principles and methods of nuclear magnetic resonance. It will apply previously learned concepts to magnetic resonance. Students should appreciate the power and versatility of this technique in a variety of applications.

- Introduction: static and dynamic aspects of magnetism, Larmor precession, relaxation to equilibrium,  $T_1$  and  $T_2$ , Bloch equations.
- Pulse and continuous wave methods: time and frequency domains. Manipulation and observation of magnetisation, 90° and 180° pulses, free induction decay.
- Experimental methods of pulse and CW NMR: the spectrometer, magnet. Detection of NMR using SQUIDs.
- Theory of relaxation: transverse relaxation of stationary spins, the effect of motion. Spin lattice relaxation.
- Spin echoes: 'violation' of the Second Law of Thermodynamics, recovery of lost magnetisation. Application to the measurement of  $T_2$  and diffusion.
- Analytical NMR: chemical shifts, metals, NQR.
- NMR imaging: Imaging methods. Fourier reconstruction techniques. Gradient echoes. Imaging other parameters.

**Books**: B P Cowan, Nuclear Magnetic Resonance and Relaxation, CUP, 1<sup>st</sup> ed. 1997 and 2<sup>nd</sup> ed. 2005. Journal and web references given during course.

### Assessment:

Written examination of 2<sup>1</sup>/<sub>2</sub> hours contributing 90%, coursework contributing 10%.

### 4515 Computing and Statistical Data Analysis

In Session 2006-7 this course will be taught at the Royal Holloway campus at Egham.

This course aims to introduce students to programming techniques using the C++ language on a Unix platform. It will also introduce students to techniques of probability and statistical data analysis and they will study applications of data analysis using C++ based computing tools.

- Introduction to C++ and the Unix operating system.
- Variables, types and expressions.
- Functions and the basics of procedural programming.
- I/O and files.
- Basic control structures: branches and loops.
- Arrays, strings, pointers.
- Basic concepts of object oriented programming.
- Probability: definition and interpretation, random variables, probability density functions, expectation values, transformation of variables, error propagation, examples of probability functions.
- The Monte Carlo method: random number generators, transformation method, acceptance-rejection method.
- Statistical tests: significance and power, choice of critical region, goodness-offit.
- Parameter estimation: samples, estimators, bias, method of maximum likelihood, method of least squares, interval estimation, setting limits, unfolding.

Books: R. Miller, An Introduction to the Imperative Part of C++, www.doc.ic.ac.uk/~wjk/C++Intro.
W. Savitch, Problem Solving with C++: The Object of Programming, 4th Ed., Addison-Wesley, 2003.
G D Cowan, Statistical Data Analysis, Clarendon Press, 1998.
R J Barlow, Statistics: A Guide to the Use of Statistical Methods in the Physical Sciences, John Wiley, 1989.

### Assessment:

Written examination of 2<sup>1</sup>/<sub>2</sub> hours contributing 70%, coursework contributing 30%.

### 4600 Stellar Structure and Evolution

Topics covered include

- Observational properties of stars, the H-R diagram, the main sequence, giants and white dwarfs.
- Properties of stellar interiors: radiative transfer, equation of state, nuclear reactions, convection.
- Models of main sequence stars with low, moderate and high mass.
- Pre- and post-main sequence evolution, models of red giants, and the end state of stars.

The course includes some exposure to simple numerical techniques of stellar structure and evolution; computer codes in Fortran.

Prerequisites: some knowledge of Fluids, Electromagnetism, Stellar Structure

**Books:** Course Notes available + R Kippenhahn and A Weigert - Stellar Structure and Evolution Springer

Assessment: Written examination of 3 hours contributing 100%

### 4601 Advanced Cosmology

- Observational basis for cosmological theories.
- Derivation of the Friedmann models and their properties.
- Cosmological tests; the Hubble constant; the age of the universe; the density parameter; luminosity distance and redshift.
- The cosmological constant.
- Physics of the early universe; primordial nucleosynthesis; the cosmic microwave background (CMB); the decoupling era; problems of the Big Bang model.
- Inflationary cosmology.
- Galaxy formation and the growth of fluctuations
- Evidence for dark matter.
- Large and small scale anisotropy in the CMB.

Prerequisites: Knowledge of Newtonian Dynamics and Gravitation, and Calculus.

### **Books:**

Assessment: Written examination of 3 hours contributing 100%

### 4602 Relativity and Gravitation

- Introduction to General Relativity.
- Derivation from the basic principles of Schwarzschild.
- Solution of Einstein's field equations.
- Reisner-Nordstrom, Kerr and Kerr-Neuman solutions and physical aspects of strong gravitational fields around black holes.
- Generation, propagation and detection of gravitational waves.
- Weak general relativistic effects in the Solar System and binary pulsars.
- Alternative theories of gravity and experimental tests of General Relativity.

**Prerequisites:** knowledge of Relativity

**Books:** 

Assessment: Written examination of 3 hours contributing 100%.

### 4603 Astrophysical Fluid Dynamics

- Fluid dynamical model in astrophysics.
- Gravitational stability, gravitational collapse.
- Stellar stability, stellar oscillations, variable stars.
- Helioseismology.
- Stellar rotation, structure of rotating stars.
- Binary stars, tidally distorted models.
- Rotationally and tidally distorted planets.

Prerequisite: An introductory course on fluid dynamics, and astrophysics.

**Book**: F. H. Shu, The physics of astrophysics, Vol II: Gas dynamics, 1992 University Science Books: Mill Valley, CA.

Assessment: 100% Written examination.

### 4630 Planetary Atmospheres

### **Comparison of the Planetary Atmospheres** (2 lectures)

The radiative energy balance of a planetary atmosphere; the competition between gravitational attraction and thermal escape processes. The factors which influence planetary atmospheres; energy and momentum sources; accretion and generation of gases; loss processes; dynamics; composition.

### **Atmospheric structure** (7 lectures)

Hydrostatic equilibrium, adiabatic lapse rate, convective stability, radiative transfer, the greenhouse effect and the terrestrial planets.

### **Oxygen chemistry** (3 lectures)

Ozone production by Chapman theory; comparison with observations; ozone depletion and the Antarctic ozone hole.

### Atmospheric temperature profiles (3 lectures)

Troposphere, stratosphere, mesosphere, thermosphere and ionosphere described; use of temperature profiles to deduce energy balance; internal energy sources; techniques of measurement for remote planets.

**Origin of planetary atmospheres and their subsequent evolution** (3 lectures) Formation of the planets; primeval atmospheres; generation of volatile material; evolutionary processes; use of isotopic abundances in deducing evolutionary effects; role of the biomass at Earth; consideration of the terrestrial planets and the outer planets.

### **Atmospheric Dynamics** (4 lectures)

Equations of motion; geostrophic and cyclostrophic circulation, storms; gradient and thermal winds; dynamics of the atmospheres of the planets; Martian dust storms, the Great Red Spot at Jupiter.

### Magnetospheric Effects (1 lecture)

Ionisation and recombination processes; interaction of the solar wind with planets and atmospheres; auroral energy input.

### Atmospheric loss mechanisms (1 lecture)

Exosphere and Jeans escape; non thermal escape processes; solar wind scavenging at Mars.

### **Observational techniques** (3 lectures)

Occultation methods from ultraviolet to radiofrequencies; limb observation techniques; in-situ probes.

### **Global warming** (3 lectures)

Recent trends and the influence of human activity; carbon budget for the Earth; positive and negative feedback effects; climate history; the Gaia hypothesis; terraforming Mars.

### Books:

J. W. Chamberlain and D. M. Hunten, "Theory of Planetary Atmospheres" Academic Press.

M. Salby, "Introduction to Atmospheric Physics", Academic Press.

J. T. Houghton, "The Physics of Atmospheres", Cambridge University Press.

### Assessment:

Written examination of  $2\frac{1}{2}$  hours contributing 100%.

### 4640 Solar Physics

### 1. Introduction

Presentation of the syllabus and suggested reading, a list of solar parameters and a summary of the topics to be treated during the course. (1)

### 2. The Solar Interior and Photosphere

Stellar Structure and Evolution. Life history of a star. Equations and results. Conditions for Convection. Arrival of the Sun on the Main Sequence. Nuclear fusion reactions. The Standard Solar Model. Neutrino production and Detection – the neutrino problem. Solar Rotation. Photospheric models and observations. Fraunhofer lines. Chemical composition. Convection and Granulation. Waves and oscillations – Helioseismology or probing the SunUs interior. (12)

### 3. Solar Magnetic Fields/Solar Activity

Sunspot observations – structure, birth and evolution. Spot temperatures and dynamics. Observations of faculae. Solar magnetism – Sunspot and Photospheric fields. Active Region manifestations and evolution. Solar Magnetic Cycle – Observations and Dynamics. Babcock dynamo model of the solar cycle. Behaviour of flux tubes. Time behaviour of the Sun's magnetic field. (4)

### 4. The Solar Atmosphere - Chromosphere

Appearance of the Chromosphere – Spicules, mottles and the network. Observed spectrum lines. Element abundances. Temperature profile and energy flux. Models of the Chromosphere. Nature of the Chromosphere and possible heating mechanisms. (4)

### 5. The Solar Atmosphere - Corona and Solar Wind

Nature and appearance of the corona. Breakdown of LTE. Ionization/ recombination balance and atomic processes. Spectroscopic observations and emission line intensities. Plasma diagnostics using X-ray emission lines. Radio emission. Summary of coronal properties. Discovery of the solar wind. X-ray emission and coronal holes. In-situ measurements and the interplanetary magnetic field structure. Solar wind dynamics. Outline of the Heliosphere. (6)

### 6. Solar Flares.

Flare observations throughout the solar atmosphere. Thermal and non-thermal phenomena. Particle acceleration and energy transport. Gamma-ray production. Flare models and the role of magnetic fields. (3)

### Assessment:

Written examination of  $2\frac{1}{2}$  hours contributing 100%.

### 4650 Solar System

- General overview/survey.
- Fundamentals: 2-body problem, continuum equations.
- Terrestrial planets: interiors, atmospheres.
- Giant planets: interiors, atmospheres.
- Satellites: 3-body problem, tides.
- Resonances and rings.
- Solar nebula and planet formation.
- Asteroids, comets and impacts.

Assessment: Written examination of 3 hours contributing 100%

**Book**: C.D. Murray and S.F. Dermott, Solar System Dynamics, Cambridge University Press.

### 4660 The Galaxy

- Introduction: galaxy types, descriptive formation and dynamics.
- Stellar dynamics: virial theorem, dynamical and relaxation times, collisionless Boltzmann equation, orbits, simple distribution functions, Jeans equations.
- The interstellar medium: emission processes from gas and dust (qualitative only), models for chemical enrichment.
- Dark matter rotation curves: bulge, disk, and halo contributions.
- Dark matter gravitational lensing: basic lensing theory, microlensing optical depth.
- The Milky Way: mass via the timing argument, solar neighbourhood kinematics, the bulge, the Sgr dwarf.

Assessment: Written examination of 3 hours contributing 100%

**References**: Shu for some basic material, Binney & Merrifield and Binney & Tremaine for some topics, plus full course notes.

### 4670 Astrophysical Plasmas

- The plasma state as found in astrophysical contexts.
- Particle motion in electromagnetic fields, cyclotron motion, drifts and mirroring, with application to the radiation belts and emission from radio galaxies.
- Concepts of magnetohydrodynamics (MHD); flux freezing and instabilities.
- The solar wind, including MHD aspects, effects of solar activity, and impact on the terrestrial environment.
- Magnetic reconnection; models and application to planetary magnetic storms and stellar flares and coronal heating.
- Shock waves and charged particle acceleration.

Assessment: Written examination of 3 hours contributing 100%

### 4680 Space Plasma and Magnetospheric Physics

### **Introduction** [1]

Plasmas in the solar system, solar effects on Earth, historical context of the development of this rapidly developing field

### Plasmas [3]

What is a plasma, and what is special about space plasmas; Debye shielding, introduction to different theoretical methods of describing plasmas

### **Single Particle Theory** [6]

Particle motion in various electric and magnetic field configurations; magnetic mirrors; adiabatic invariants; particle energisation

### Earth's Radiation Belts [3]

Observed particle populations; bounce motion, drift motion; South Atlantic Anomaly; drift shell splitting; source and acceleration of radiation belt particles; transport and loss of radiation belt particles

### Introduction to Magnetohydrodynamics [3]

Limits of applicability; convective derivative; pressure tensor; continuity equation; charge conservation and field aligned currents; equation of motion; generalised Ohm's law; frozen-in flow; magnetic diffusion; equation of state; fluid drifts; magnetic pressure and tension

### The Solar Wind [3]

Introduction, including concept of heliosphere; fluid model of the solar wind (Parker); interplanetary magnetic field and sector structure; fast and slow solar wind; solar wind at Earth; coronal mass ejections

### The Solar Wind Interaction with Unmagnetised Bodies [2]

The Moon; Venus, Comets

### The Solar Wind and Magnetised Bodies (I) [4]

Closed Magnetosphere Model

The ring current, boundary currents; shape of the magnetopause; corotation; convection driven by viscous flow

### The Solar Wind and Magnetised Bodies (II) [3]

Open Magnetosphere Model, Steady State

Magnetic reconnection; steady state convection; currents and potentials in an open magnetosphere; the magnetotail; the plasmasphere; the aurorae

### The Solar Wind and Magnetised Bodies (III) [2]

Open Magnetosphere Model, Non-Steady State

Phases of a substorm; Substorm current systems and unanswered questions about substorms; magnetic storms; dayside reconnection.

**Books**: M.Kivelson and C.T.Russell, Introduction to space physics, Cambridge University Press, W.Baumjohann and R.Treumann, Basic space plasma physics, Imperial College Press

Assessment: Written examination of  $2\frac{1}{2}$  hours contributing 100%.

**Prerequisites**: While the course is essentially self-contained, some knowledge of basic electromagnetism and mathematical methods is required. In particular it is assumed that the students are familiar with Maxwell's equations and related vector algebra.

### 4750 Image Capture and Sensor Technology

- **The Human Observer** (3 Lectures) The eye, spectral sensitivity, target acquisition.
- Electromagnetic Radiation (3 Lectures) Properties, Sources, photon statistics, Planck's Law, radiation transfer, atmospheric windows
- Ideal Detection (3 Lectures) Quantum limit of detection, signal to noise ratios, detectivities, noise equivalent powers.
- **Detector Principles** (3 Lectures) Photon phenomena, thermal effects, semiconduction.
- **Detector Types I** (3 Lectures) Photo-emissive, photo-conductive, photo-voltaic.
- **Detector Types II** (3 Lectures) Thermal, thermopiles, bolometers, pyro-electric devices.
- Noise Processes (3 Lectures) Physical origins of noise, shot noise, background noise, amplifier noise, dark currents, flicker noise, generation and recombination noise, the vacuum photodiode
- **Signal Multiplication** (3 Lectures) Photomultipliers, CRTs, image intensifiers, avalanche effects.
- Multi-element Detectors (3 Lectures) CCDs, SPRITE, infra-red imaging modes, sampling two dimensional signals.
- **Detector systems** (3 Lectures) optical transfer functions, optical elements and aberrations.
- Selected Applications (3 Lectures) X-ray detection, FLIR, SAR.

**Prerequisites**: –Mathematical skills at a physical sciences level, Physics at a level of a science based undergraduate.

### **Reading List:**

1. Springer Optical Science Series, R H Kingston, Detection of Optical and Infra-red Radiation, Vol 10 Ed David L MacAdam, Springer, 1978, ISBN 3-540-08617-X (not currently in print, but in libraries)

2. Semiconductor Detector Systems, Helmuth Spieler, (Oxford University Press, 2005; 2nd printing 2006). ISBN: 0198527845

3. http://www-physics.lbl.gov/~spieler/

### Assessment:

Written examination of 3 hours contributing 90%, coursework contributing 10%.